

Practice – 4.1 Angles and Angle Measures

1. Convert each angle measure to **radians**.

$$\begin{aligned} \text{a) } 10^\circ & \left(\frac{\pi}{180^\circ} \right) \\ & = \frac{\pi}{18} \end{aligned}$$

$$\begin{aligned} \text{b) } -240^\circ & \left(\frac{\pi}{180^\circ} \right) \\ & = -\frac{4\pi}{3} \end{aligned}$$

$$\begin{aligned} \text{c) } 390^\circ & \left(\frac{\pi}{180^\circ} \right) \\ & = \frac{13\pi}{6} \end{aligned}$$

$$\begin{aligned} \text{d) } -120^\circ & \left(\frac{\pi}{180^\circ} \right) \\ & = -\frac{2\pi}{3} \end{aligned}$$

2. Convert each angle measure to **degrees**.

$$\begin{aligned} \text{a) } \frac{\pi}{5} & \left(\frac{180^\circ}{\pi} \right) \\ & = 36^\circ \end{aligned}$$

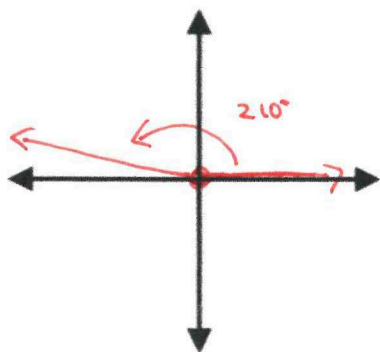
$$\begin{aligned} \text{b) } \frac{5\pi}{3} & \cdot \left(\frac{180^\circ}{\pi} \right) \\ & = 300^\circ \end{aligned}$$

$$\begin{aligned} \text{c) } -\frac{\pi}{2} & \left(\frac{180^\circ}{\pi} \right) \\ & = -90^\circ \end{aligned}$$

$$\begin{aligned} \text{d) } 4\pi & \left(\frac{180^\circ}{\pi} \right) \\ & = 720^\circ \end{aligned}$$

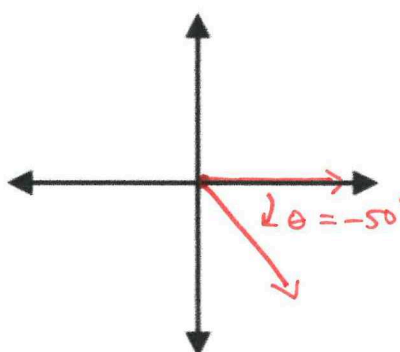
3. **Sketch** each angle in standard position. State the reference angle.

a) 210°



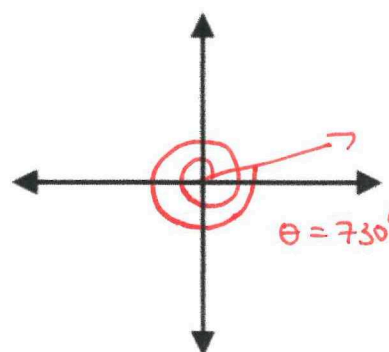
Reference Angle: $\theta_r = 30^\circ$

b) -50°



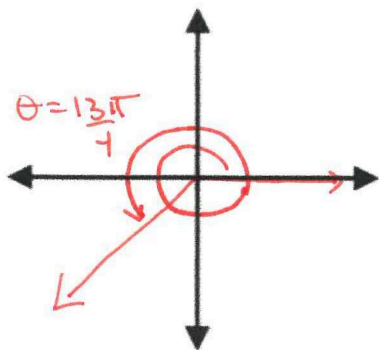
Reference Angle: $\theta_r = 50^\circ$

c) 730°

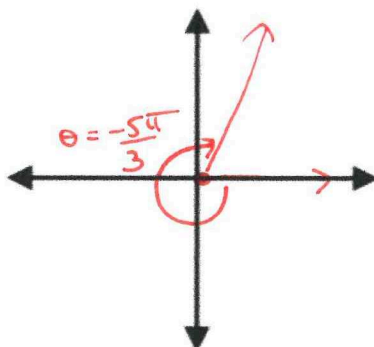


Reference Angle: $\theta_r = 10^\circ$

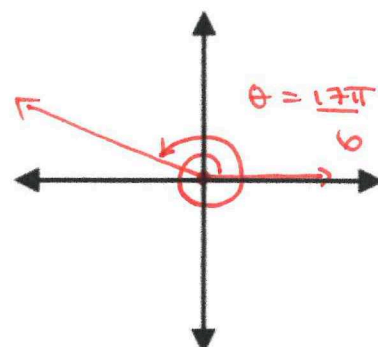
d) $\frac{13\pi}{4}$

Reference Angle: $\theta_r = \pi/4$

e) $-\frac{5\pi}{3}$

Reference Angle: $\theta_r = \pi/3$

f) $\frac{17\pi}{6}$

Reference Angle: $\theta_r = \pi/6$ 4. Determine one positive and one negative **coterminal angle** for each of the following.

a) 30°

$390^\circ, -330^\circ$

b) 135°

$495^\circ, -225^\circ$

c) -75°

~~285~~
 $285^\circ, -435^\circ$

d) -148°

$212^\circ, 508^\circ$

5. Determine one positive and one negative **coterminal angle** for each of the following.

a) $\frac{\pi}{8}$

$\pm \frac{16\pi}{8}$
 $\frac{17\pi}{8}, -\frac{15\pi}{8}$

b) $-\frac{\pi}{7}$

$\pm \frac{14\pi}{7}$
 $-\frac{15\pi}{7}, \frac{13\pi}{7}$

c) $-\pi$

$\pm 2\pi$
 $-3\pi, \pi$

d) $\frac{4\pi}{9}$

$\pm \frac{18\pi}{9}$
 $\frac{22\pi}{9}, -\frac{14\pi}{9}$

Practice – 4.2 Unit Circle

6. Determine if the following point $\left(\frac{12}{13}, \frac{5}{13}\right)$ lies on the **unit circle**.

Explain how you know.

$$\left(\frac{12}{13}\right)^2 + \left(\frac{5}{13}\right)^2$$

$$\frac{144}{169} + \frac{25}{169}$$

$$\frac{169}{169} = 1$$

The point satisfies
the equation of
the unit circle

$$x^2 + y^2 = 1$$

and \therefore is on the
unit circle.

7. The following points lie on the unit circle. Determine the **missing coordinate** satisfying the given conditions.

a) $\left(\frac{2}{3}, y\right)$ in QIV

$$x^2 + y^2 = 1$$

$$\left(\frac{2}{3}\right)^2 + y^2 = 1$$

$$y^2 = 1 - \frac{4}{9}$$

$$y^2 = \frac{9}{9} - \frac{4}{9}$$

$$y = \pm \sqrt{\frac{5}{9}}$$

$$y = -\frac{\sqrt{5}}{\sqrt{9}} = -\frac{\sqrt{5}}{3}$$

b) $\left(x, \frac{4}{5}\right)$ in Q2

$$x^2 + y^2 = 1$$

$$x^2 + \left(\frac{4}{5}\right)^2 = 1$$

$$x^2 + \frac{16}{25} = 1$$

$$x^2 = \frac{25}{25} - \frac{16}{25}$$

$$x^2 = \frac{9}{25}$$

$$x = \pm \sqrt{\frac{9}{25}}$$

$$x = -\frac{3}{5}$$